## 2D Elastic Collision Problem: Walkthrough

Name: $\qquad$ Date: $\qquad$
A mass $m_{1}$ traveling to the right with a speed $\mathrm{v}_{1}$ makes a glancing collision with a mass $m_{2}$ initially at rest. After the collision the masses have speeds $v_{1 f}$ and $v_{2 f}$ and move in directions $\theta_{1}$ and $\theta_{2}$, as shown below.


The problem here is to find the final velocity of mass 2 after the collision. Proceed as follows:
(a) Is kinetic energy conserved? (You are not told that the collision is elastic, so don't make this assumption. The fact that the balls rebound doesn't make the collision perfectly elastic.)
(b) Is momentum conserved? (Momentum is always conserved if you can neglect external forces during the collision.)
(c) Momentum is a vector. This means that momentum must be conserved for the $x$ direction and for the $y$-direction. What is the total $x$-component of momentum before the collision? What is the total $y$-component before the collision?

$$
\begin{aligned}
& p_{x}= \\
& p_{y}=
\end{aligned}
$$

(d) What are the total $x$ - and $y$-components of momentum after the collision? (Think conservation of momentum.)

$$
\begin{aligned}
& \mathrm{P}_{\mathrm{xf}}= \\
& \mathrm{P}_{\mathrm{yf}}=
\end{aligned}
$$

(e) What are the $x$ - and $y$-components of momentum of mass 1 after the collision? (You know its speed and direction, so you can calculate its momentum.)

$$
\begin{array}{ll}
\mathrm{p}_{1 \mathrm{xf}}= & = \\
\mathrm{p}_{1 \mathrm{yf}}= & = \\
\hline
\end{array}
$$

(f) What are the $x$ - and $y$-components of the momentum of mass 2 after the collision? Use the fact that the total momentum is the sum of the momenta of each particle.

$$
\begin{aligned}
& p_{x f}=p_{1 x f}+p_{2 x f} \\
& p_{y f}=p_{1 y f}+p_{2 y f}
\end{aligned}
$$

So,

$$
\mathrm{p}_{2 \times f}=
$$

$\qquad$

$$
\mathrm{p}_{2 \mathrm{yf}}=
$$

$\qquad$
(g) From $p_{2 x f}$ and $p_{2 y f}$ find $v_{2 x f}$ and $v_{2 y f}$.

$$
v_{2 x f}=p_{2 x f} / m_{2}=
$$

$\qquad$ , $\mathrm{v}_{2 \mathrm{yf}}=\mathrm{p}_{2 \mathrm{yf}} / \mathrm{m}_{2}=$ $\qquad$
(h) Now find $v_{2 f}$ and $\theta_{2}$. (include a diagram)

$$
\begin{aligned}
& \mathrm{V}_{2 \mathrm{f}}= \\
& \theta_{2}=
\end{aligned}
$$

