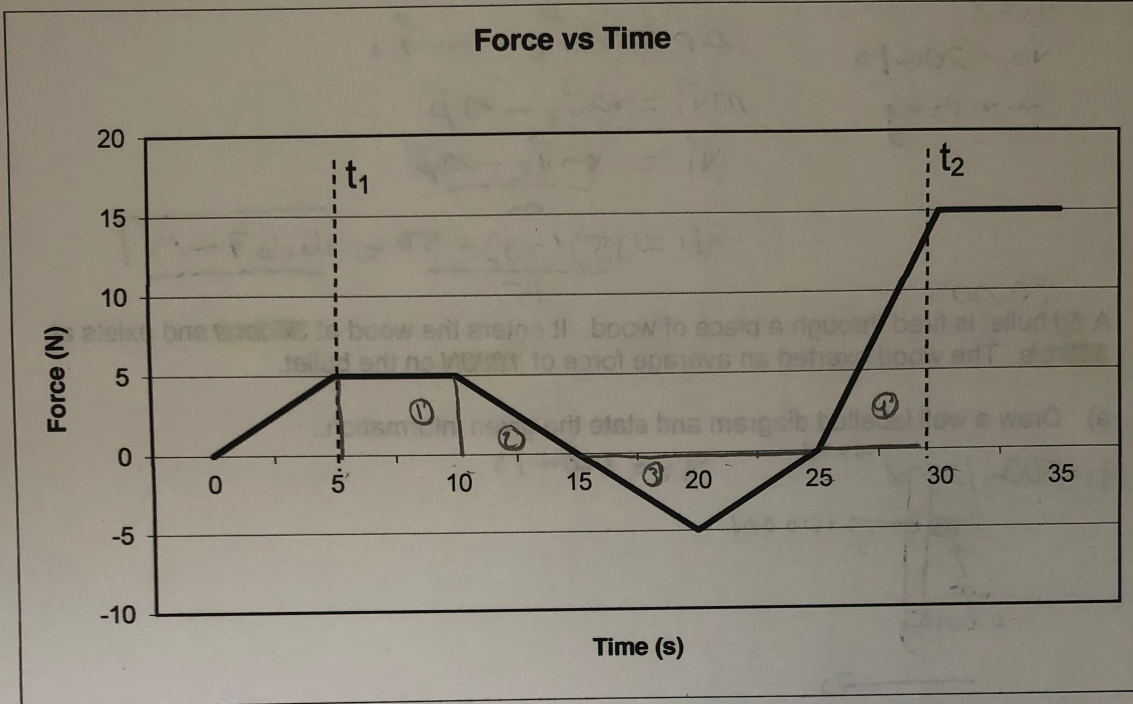


Momentum & Impulse

Name: Madison Dempster

Date: April 1/20

1. A **15kg** object has the following time variant force $F(t)$ acting on it.



The object has a final velocity, $v(t_2)$, of **20m/s**. Determine

a) The impulse from t_1 to t_2 .

$$\vec{I} = \sum \vec{F}_a \Delta t = \Delta \vec{p}$$

$$|\vec{I} = 50 \text{ N}\cdot\text{s}|$$

from t_1 to t_2

Area: ① $5 \times 5 = 25 \text{ N}\cdot\text{s}$

② $\frac{5 \times 5}{2} = 12.5 \text{ N}\cdot\text{s}$

③ $-\frac{5 \times 10}{2} = -25 \text{ N}\cdot\text{s}$

④ $\frac{5 \times 15}{2} = 37.5 \text{ N}\cdot\text{s}$

$\Delta T = 50 \text{ N}\cdot\text{s}$

- b) The average force over the time interval indicated in a)

$$\vec{I} = \sum \vec{F}_{av} \Delta t$$

$$\sum \vec{F}_{av} \Delta t = \frac{\vec{I}}{\Delta t} = \frac{50 \text{ N}\cdot\text{s}}{25 \text{ s}} = \underline{2 \text{ N}}$$

- c) The initial velocity of the object at t_1 .

$$v_1 = ?$$

$$v_2 = 20 \text{ m/s}$$

$$m = 15 \text{ kg}$$

$$\Delta \vec{p} = m\vec{v}_2 - m\vec{v}_1$$

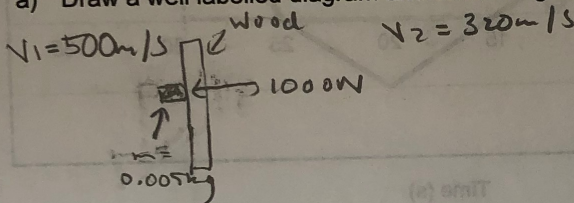
$$m\vec{v}_1 = m\vec{v}_2 - \Delta \vec{p}$$

$$\vec{v}_1 = \frac{m\vec{v}_2 - \Delta \vec{p}}{m}$$

$$v_1 = \frac{(15)(20) - 50}{15} = \underline{16.67 \text{ m/s}}$$

2. A 5 g bullet is fired through a piece of wood. It enters the wood at 500 m/s and exits at 320 m/s . The wood exerted an average force of 1000 N on the bullet.

- a) Draw a well labelled diagram and state the given information..



- b) Determine the change in momentum.

$$\Delta \vec{p} = m\vec{v}_2 - m\vec{v}_1$$

$$= (0.005)(320) - (0.005)(500)$$

$$\Delta \vec{p} = \underline{-0.9 \text{ N}\cdot\text{s}}$$

- c) Determine how long the bullet was in the wood for.

$$\sum \vec{F} = m\vec{a}$$

$$a = \frac{F}{m} = \frac{-1000}{0.005} = -200,000 \text{ m/s}^2$$

$$v_2^2 = v_1^2 + 2a d$$

$$d = \frac{v_2^2 - v_1^2}{2a} = \frac{(320)^2 - (500)^2}{2(-200,000)} = \underline{+0.369 \text{ m}}$$

- d) Determine how thick the piece of wood is.

$$\Delta \vec{p} = \sum \vec{F}_{av} \Delta t$$

$$\Delta t = \frac{\Delta \vec{p}}{\sum \vec{F}_{av}} = \frac{-0.9 \text{ N}\cdot\text{s}}{-1000} = \underline{0.0009 \text{ s}}$$