Springs & Hooke's Law – Investigation



Purpose: To investigate and discover Hooke's Law: To describe the relationship between the force exerted on a spring and the resulting stretch. The amount of energy stored in the spring will also be determined.

Outcomes:

Student should be able to ...

- Describe mathematically the relationship between the force and stretch of a spring
- Understand what is meant by spring constant and to be able to determine the spring constant.
- Determine the amount of energy stored in the stretched spring.

Procedure & Analysis:

- 1. Go to the <u>applet website</u>.
- 2. Watch the <u>video explanation</u> of the investigation and how to use the applet.
- 3. Complete the tables for two different spring constants (listed at the top of the table)
- 4. Graph both sets of data on the Force vs. Stretch graph provided. Use a scatter plot and draw a line of best fit through both lines.
- 5. Calculate the slope of both lines (including units)
- 6. Answer the discussion questions in full detail showing all work.

Data Collection:

Complete the tables using the applet.

Table 1: Spring Constant (200 N/m)

Force (N)	Stretch, Δx (m)
0	
10	
20	
30	
40	
50	
60	

Table 2: Spring Constant (600 N/m)

Force (N)	Stretch, Δx (m)
0	
10	
20	
30	
40	
50	
60	

Analysis:

Graph both sets of data and label the axis. Stretch on x-axis and Force on y-axis.

- 1. Create it as a scatter plot and draw the line of best fit (colour code and/or label each line as well)
- 2. Calculate the slope of each line (include units) compare the applet.



Discussion Questions & Analysis:

- 1. Describe the relationship between the force and stretch of the spring.
- 2. On the applet try compressing the spring (negative force) with the same values as the table. What do you notice about the COMPRESSION distance compared to the STRECTH distance?
- 3. The **spring constant** is the slope of the best-fit line and is given the symbol *k*. Different springs have different *k* values. What are the values and the units of *k* from your experiments?

Spring 1:

Spring 2:

- 4. Assume you have a slinky (very small spring constant) and a car suspension spring (very large spring constant. You apply the same force to both in order to stretch them. Which would stretch more?
- 5. Resistance band workout bands come in different colours. There are many different brands one brand has the following coding system. Which band would have the lowest k value and which would have the largest k value? Indicate on the chart.

Color	Resistance
Tan	XX-Light
Yellow	X-Light
Red	Light
Green	Medium
Blue	Heavy
Black	X-Heavy
Silver	XX-Heavy
Gold	XXX-Heavy

- 6. Using the 600 N/m spring constant from your investigation calculate / predict the amount of stretch that would get if you applied a force of 45 N. Check with the applet.
- 7. Using the 600 N/m spring constant from your investigation calculate / predict the amount of pushing force needed to compress the spring by 9.5 cm. Check with the applet.

8. You have a spring with a *k*=440 N/m, and you stretch it by 5.2 cm. Calculate the force applied to do this. Check with the applet.

Consolidation:

Hooke's Law

For an **ideal spring**, the force needed to stretch of compress a spring by some distance, x, scales linearly with respect to that distance. If a spring is overstretched or over-compressed it will deform and the relationship becomes non-linear and the spring is considered non-ideal.

$$F_s = -k\Delta x$$

*The negative sign simply indicates that the force the spring is opposite to the applied force (Newton's 3rd Law)

- 1. A spring has a spring constant of 256 N/m and is stretched 32 cm. Calculate the force acting on the spring?
- 2. A force of 20 N is applied to a 12.5 N/m spring. Calculate the stretch on the spring.

Energy Stored in a Spring

The area under the curve on the graph represents the energy stored in the spring at that given stretch.

1. Using the 200 N/m spring from the investigation – using the graph, shade the area from 0 to 0.20m under the line. Calculate the area of the triangle. The units will be $N \cdot m = J$ (*Joules*)

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Equation: The energy stored in the spring can also be determined by:

$$E_s = \frac{k\Delta x^2}{2}$$

2. Using the equation above. Calculate the energy stored in the spring where the stretch is 0.20 m and the spring constant is 200 N/m. How does this value compare to the area you calculated?

Questions:

1. A spring with a spring constant of 350 N/m is stretched 0.45 m. Determine the force of the spring and the amount of stored energy in the spring.

2. A spring is stretch 35 cm and the amount of energy stored in the spring was determined to be 160 J. Determine the spring constant of the spring.